

Methods for scaling a large member base

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February 16, 2006

Abstract

The technical challenges of scaling websites with large and growing member bases, like social networking sites, are numerous. One of these challenges is how to evenly distribute the growing member base across all available resources. This paper will explore various methods that address this issue. The techniques used in this paper can be generalized and applied to various other problems that need to distribute data evenly amongst a finite amount of resources.

1 Problem

Some websites, like social networking sites, are challenged with the task of trying to scale their exponentially growing member base. How websites deal with this issue while keeping up with demand varies. Some websites chose to have a single large database. Then when usage grows they tend to invest large sums of money on a massive multi-processor system. Other sites choose to distribute their members across clusters of inexpensive database servers. This, in theory, will help to scale the site by adding more database servers when usage increases. However, the scheme used to segment and distribute the members varies from site to site.

One common method used to distribute a sites member's is to segment the members based on their user name. For example, with a Web site that contains blogs, 26 different blog databases can be created, based on alphabetical characters, such as $\{a, b, c, \dots, z\}$ all with identical schematics. Then members can be placed into a database segmented by the first letter of their user name, allowing for a relatively intuitive and easy way to distribute the data. Moreover, if the site requirements include scalability, in theory, 26 different database servers can be set up, with each server handling its own letter-group. However, the allocation of the data distribution with such a scheme will not actually result in even distribution given the actual usage of letters, and such unevenness will be further augmented when scaled to a very large member base. To make effective use of resources a finer method of distributing this data evenly is desirable; this method should ensure, for example, that each database has as close to the same number of records as possible.

1.1 Solution consideration and constraints

This analysis will find a simple algorithm that will evenly distribute a large growing population of members across a set of finite servers. Given the complexity of this problem, measurements for determining the effectiveness of an algorithm need to be established. One useful measurement is the Standard Deviation of the distribution¹; this measurement describes how evenly spread out the data is². Thus, the optimal algorithm will produce a small deviation.

Computational and functional needs of the algorithm also need to be considered. The optimal algorithm should have the following attributes:

1. Independence from external data sources - it should require only the member's user name string and no external data. This is mainly for simplicity and ease of implementation.
2. Simple and lightweight - it should not require expensive calculations.
3. Platform agnosticity and independence.
4. Easily implementable in scripted languages. Scripting languages, such as PHP and Perl, are very popular and commonly used for Web applications. Thus, an ideal algorithm would be simple enough to implement within them.
5. Must not require the use of large file system subdirectory trees. Some filesystems, and NAS devices, have limits as to the amount of sub directories allowed and the algorithm must not exceed them. Also, for performance reasons, smaller directory trees are desired.
6. Truly scalable, to very large numbers (at least one billion).
7. Must be a one-to-one (i.e. injective) function (for example: $\forall a, b \in f$ we have $f(a) = f(b) \Rightarrow a = b$).

2 Letter based distributions

For this paper, I am going to use Fotolog.net as a real world example³. As of writing, Fotolog.net has more than 1 Million registered members. Each member has the ability to post photos with captions, post entries into guestbooks, and create lists of friends and favorites. The members data is spread across several different clusters of database and NAS servers. Currently, members are distributed based on the first character of the member's user name. For example, if the member's user name is "frankie" the member's photo captions are

¹In this paper, the mean of a distribution refers to the ideal mean. As an example, given 10 buckets and 20 users, the ideal mean is 2 users per bucket.

²http://en.wikipedia.org/wiki/Standard_deviation

³Fotolog.net is a photo sharing community. For more information please visit: <http://www.fotolog.net>.

Graph: D1

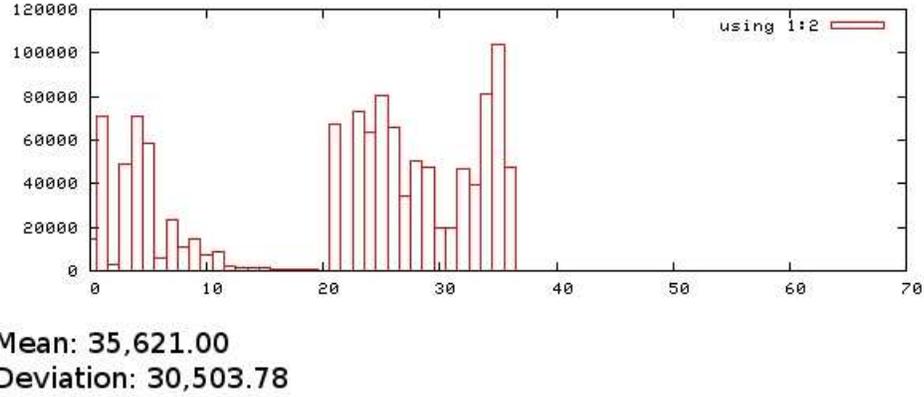


Figure 1: Distribution of the first level.

stored in a table in the 'F' photo database. Because Fotolog.net user names are comprised of 37 distinct alpha numeric characters⁴, this creates 37 unique data sources, a data source per every user name character allowed.

Similar to the databases, the photos are stored on a NAS file system and the photos are distributed across the NAS servers based on the first character of the member's user name. However, unlike the databases, the photos are kept in a directory structure that can have up to six sub directories. These sub directories are created based on the expansion of the characters in the member's users name. For example, the photos for the member "frankie" would be stored on the NAS server in the following directory structure:

```
<root dir>/f/r/a/n/k/i/frankie/my_photos
```

The graph D1⁵ shows Fotolog's first level distribution of member's user names. Graph D2⁶ shows the distribution of Fotolog's second level letter expansion. The graph D3⁷ shows the distributions of Fotolog's third level expansion. All three graphs are based on 1,188,968 user names⁸.

⁴User names are not case sensitive and include the numerals 0 through 9, alphabet characters a through z, and the underscore character (_).

⁵The graph was calculated by mapping the allowed characters (0-9,a-z,_) into integers 0 - 37 then calculating $x \bmod 37$ where x is the first character in the user's name.

⁶The graph was calculated by mapping the allowed characters (0-9,a-z,_) into integers 0 - 37 then calculating $x_i \bmod 37, i \in \{0, 1\}$ where i specifies the character index in the user's name.

⁷The graph was calculated by mapping the allowed characters (0-9,a-z,_) into integers 0 - 37 then calculating $x_i \bmod 37, i \in \{0, 1, 2\}$ where i specifies the character index in the user's name.

⁸All current registered members as of April 2, 2005.

Graph: D2

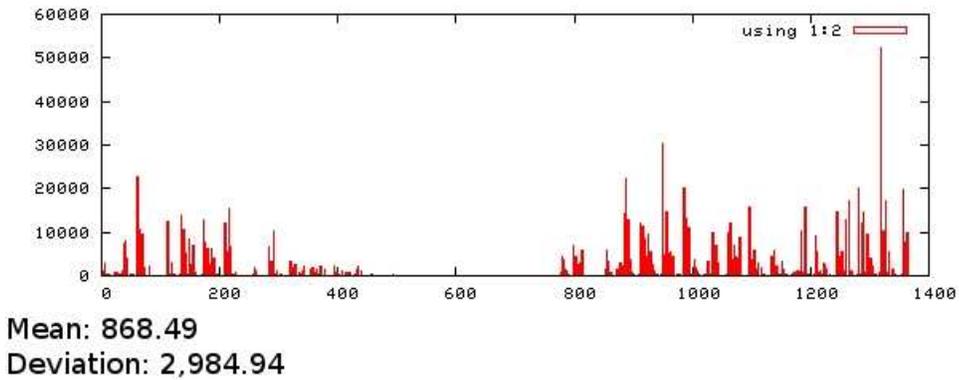


Figure 2: Distribution of the second level letter expansion.

Graph: D3

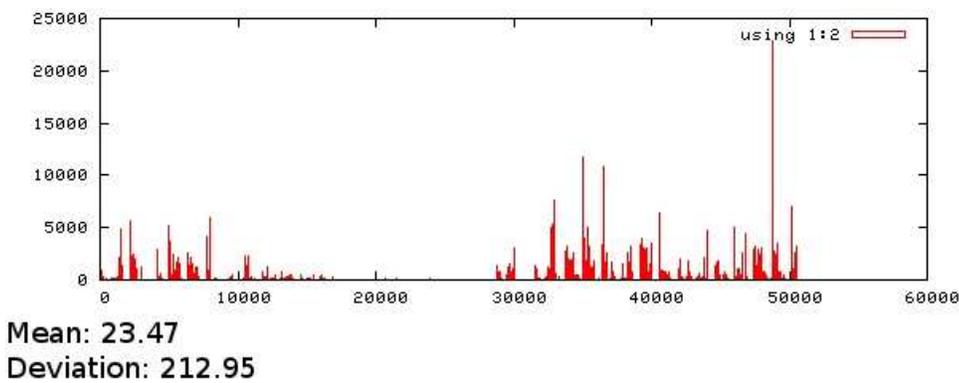


Figure 3: Distribution of the third level letter expansion.

The distribution shown in graph D1 has a mean of 35,651 with a standard deviation of 30,504. Because the mean and the standard deviation are almost equivalent, the letter based distribution algorithm can be determined to be less than optimal at this level. In fact, if one were to rearrange the letters one could create a graph that resembles the Gaussian distribution of random numbers. This would suggest, interestingly enough, that first letter usage will grow in a Gaussian distribution like manner. Not very surprising if one considers the members names as random strings. Then this growth pattern is expected.

Graph D2 seems to indicate that the distribution will become less ideal with further letter expansions. The deviation is almost four times the mean. The graph D3 confirms that skewing of data will become more extreme the further down the directory structure is traversed. In this case the mean is nearly ten times smaller than the deviation. Some buckets directories contain almost 25,000 objects while others contain almost zero. From these results, I did not see any reason to continue to create graphs of the distribution further down. It is obvious from these graphs that the letter based method is not very efficient. However, it does satisfy many of our constraints. Still, we should be able to improve on this.

3 Other possible methods

An obvious lesson from Fotolog's letter based distribution is that common letters used in names will tend to skew the distribution. For example, M and D are very common first letters in names and the graph D1 clearly shows that these letters do indeed skew the distribution. Therefore, algorithms such as b-trees, heaps, or any other sorting algorithms, when based on the characters of the member's user name, will also result in very uneven distributions, mainly because such algorithms require subsequent weighting or ordering of data for improved search results. Not to mention, these algorithms don't make much sense in this context.

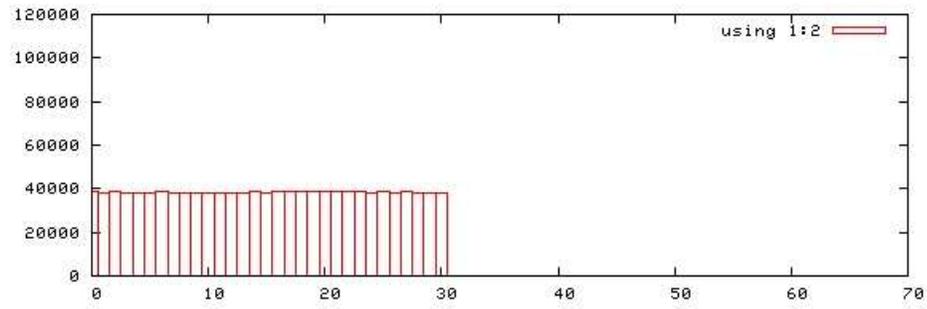
3.1 ASCII sum algorithm

A possible algorithm choice is to sum up the ASCII values of the letters in the member's user name. For example, the user name bob has the following ASCII values: 98, 111, 98. Its ASCII sum would then be: $98+111+98 = 307$. We can then use this sum to distribute the user by calculating: $x = n \text{ mod } S$. Where, n is the ASCII sum, S is a constant representing the number of resources (also referred to as the bucket size), and x would then be the data location to store that member. To calculate the second level data location we would have to modify the calculation to avoid producing the same number and lumping the data together into single directory below the top level one ⁹. One simple way we can do this is by removing the first letter in the member's user name. For example, the member bob would have a second level calculation by summing the ASCII values of 'o' and 'b'.

Graph N1 was created by calculating $x_1 = n_1 \text{ mod } 31$. Graph N2 was created by by calculating $x_2 = n_2 \text{ mod } 33$ where n_1 is the ASCII sum of the entire user name string and n_2 is the ASCII sum of the member's user name string minus the first character. The bucket sizes were chosen mostly by experimentation. Prime numbers, in this case, work most ideally because prime numbers will not have common factors that could skew the distribution.

⁹If the calculation $a = x \text{ mod } 64$ is computed, and then $b = x \text{ mod } 64$ is computed using the same x value, the result is $a = b$, meaning that the users will be lumped into a second level directory with the same number as the top directory.

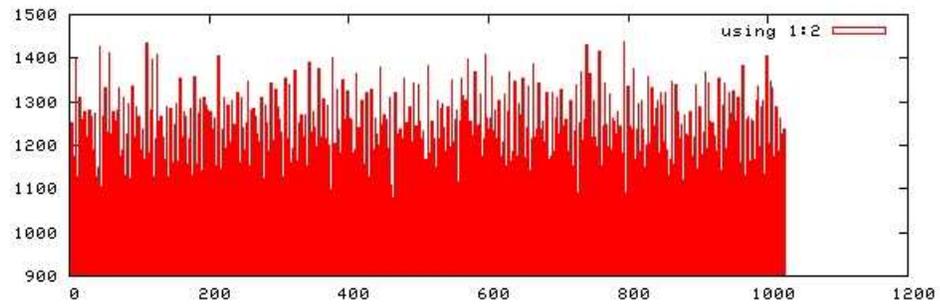
Graph: N1



Mean: 38,353.80
Deviation: 228.88

Figure 4: Graph N1.

Graph: N2



Mean: 1,162.24
Deviation: 102.76

Figure 5: Graph N2.

The results of Graph N1 appears quite promising; the deviation is only about 0.006 of the mean. Graph N2 also looks very promising; the deviation is only about 0.09 of the mean. However, common letter combinations will slightly skew the distribution. For example, the names “Jonathan, Nathan, Ethan, Nate, Natile” all have similar letter combinations. Thus, because addition is commutative, these names will tend to have similar factors and values when summed. This might get worse over time, still, this approach seems to be superior to the letter expansion approach, however, we must continue our search for a more efficient algorithm.

3.2 Mapping algorithms

We could try to create a mapping scheme to scale the member base. For example, we could keep an increasing counter and for each member we could assign them the value of the counter when they signed up. That way we could map a unique integer to a specific user name. We could then segment the user names based on integer ranges - also referred to as buckets. For example, members in the integer range $[N_1, N_2]$ could be placed in to a bucket on database D_1 , and so on. Since this distribution does not consider the members user name string, and since the number line is smooth, it could possibly provide us with a nice even distribution. However, the members user name is now dependant on an external data source. For this method to work, in some form, there must exist a table that matches a members user name to their integer I.D. This violates our first constraint and might cause a slight performance hit when we go to look up the members integer I.D. Even still, maybe we should toss out the first constraint and keep this method? It seems to solve our problem.

I would agree that this approach is attractive at first but it has some issues. One issue is that we have to be careful not create a bucket size too large, otherwise, we will have servers with almost no members on them and others with full buckets. For example, if we have 24 servers, 1 million members, and if we decide to create a bucket size of 50,000. This would fill up the first 20 servers while the other 4 are idle. Now let's say we only have 20 servers and, the same, 1 million members. Once again, if we decide to create a bucket size of 50,000 all our servers have an even amount of members. However, where do we place member 1,000,001? At some point in the future, as the member base grows, we will have a single server with 99,999 members. While the other 19 have only 50,000. This does seem to be an ideal situation, but we can make further improvements.

An obvious approach to improve this situation is to create smaller buckets and spread these across the servers using a simple calculation. For example, if we have 20 servers, 1 million members, and a bucket size of 10,000, we can distribute the resulting 100 buckets by placing 5 onto each server. Then, as our member base grows, at some point a single server will only have 9,999 more members than the others ¹⁰. If this is not acceptable, more adjustments can be

¹⁰This will happen when we have 1,049,999 members.

made to find the optimal bucket size. The end result is we only need to perform a simple calculation to find our server like: $x = n \bmod S$ ¹¹. Where n is the user ID, S is the bucket size, and x is the server we want. We have a nice bucket size, a fairly even distribution, and a simple calculation to locate our server. However, we may still have issues with growth and activity.

As the member base and level of activity grows, some buckets may have more activity than others. These buckets with increased activity are called hot spots. For example, lets say members inside bucket B_i become very active and so do the members inside bucket B_j . Now, lets say that both of the buckets are stored onto a single server S_k and the server is becoming strained and non-responsive. The first instinct is to move one of these active buckets off of server S_k onto another. However, in doing this you could break your calculation required to locate the server. Over time these hot spots could continue to develop and erode away at the bucket size and distribution. This will eventually force a double look up. The first to find the users I.D. and the second to locate the bucket and the server it's located on. The end result is a fragmented and hard to maintain distribution of buckets. An algorithm for this approach might exist. However, I cannot seem to come up with one that meets the initial constraints and is elegant.

3.3 Hashing algorithms

One thing we learn from the sum and mapping approaches is that it would be beneficial if we could find some way to map a member into the integer number line. This mapping should only use the members user name, as per our constraints, and still produce some kind of integer value that does not skew the distribution with common letter combinations. One such group of algorithms that might solve our problem are hashing algorithms. One advantageous property of hashing algorithms is that each unique input should produce a unique output¹²¹³. This should help us to avoid problems with similar letters used in member's user names.

Most scripting languages have built in hashing functions, however, these hashing functions are not standardized. Different scripting languages could have different hashing implementations. Thus, if we computed the hash of a string in one language and then we tried to compute the hash of that same string in another language they might not match. Also, it is possible that a given language might change its hashing implementation. Instead we should find a standard and widely implemented hashing function.

One excellent candidate is MD5. We could compute the MD5 sum for the member's user name. Then, the we can distribute the data based on that result. For example, the name "frank" will have the following MD5 sum:

¹¹I have seen another approach in which the servers are mapped onto the unit circle. The end result is similar since $n \bmod S$ is cyclical.

¹²Hash algorithms do not always produce unique output for every unique input. However, we will not concern our selves with ways to defeat hashing algorithms in this paper.

¹³http://en.wikipedia.org/wiki/Hash_function

```
MD5(frunk) = d268c8fe7f154537c2c9ed60a0b8f2fd
```

We could chose the first character from the MD5 sum (in this case “d”), and then distribute the data based on this character. However, MD5 returns its results in ASCII hexadecimal format. Thus, the first character will only have 16 different values, forcing the top level bucket size to be too small because the limit can be extended to only 16 different data sources. Using the first two characters of the MD5 sum may appear to be a solution, but that will yield 255 top level buckets, which might be excessive because some of these data sources could be file system mounts¹⁴.

Another approach is to take these first two characters and mod them by 64. This would create a total of 64 data sources, which is easy to maintain and, if the data is spread out evenly, 1 billion objects would only create about 16 million entries per data source ($\frac{2^{30}}{2^6} = 2^{24}$). The graph M1 demonstrates the distribution of this algorithm.

Graph: M1

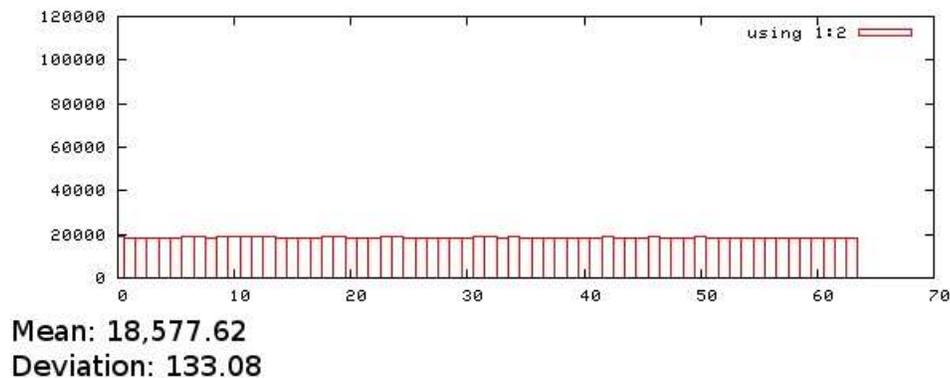


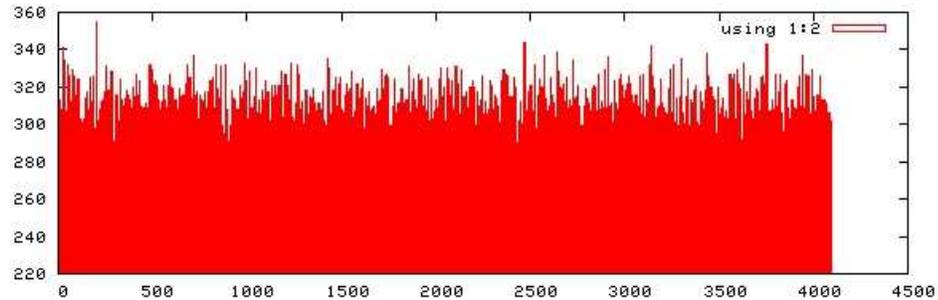
Figure 6: Graph of the first level of the MD5 distribution.

As seen from the graph M1, the MD5 algorithm provides a nice and even distribution. The average bucket holds around 18,000 objects and the deviation is about 0.007 of the mean. This algorithm appears to perform ideally for the top level directories and database distribution. However, consider the subdirectories.

When calculating the value for the second level, the currently calculated value for the top level directory must not be reused; otherwise, all the data will end up lumped together in a single directory below the top level directory. The second level is calculated using the next two digits from the MD5 string (places 2 and 3) for the mod 64 calculation. Graph M2 shows this data.

¹⁴This is a purely arbitrary restriction; as a Unix administrator keeping track of more than 254 mount points on every server is simply not an appealing option.

Graph: M2



Mean: 290.28
Deviation: 16.85

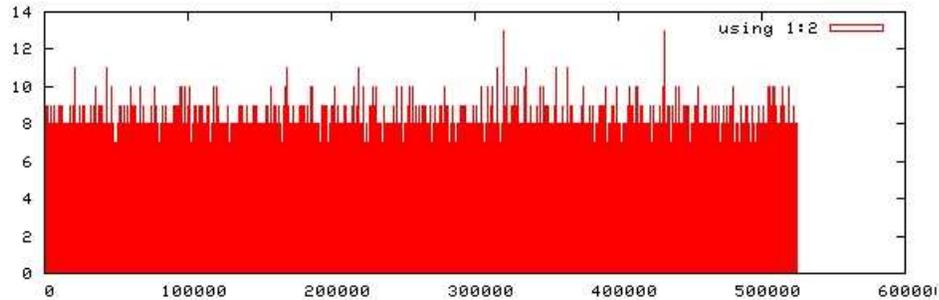
Figure 7: Graph of the second level of the MD5 distribution.

The graph M2 shows that although the results are not as optimal as the top level directory, the deviation is only about 0.06 of the mean. Each bucket has about 300 objects and could easily handle many more without going beyond file system limits¹⁵. The same approach can also be used for the final directory level; the next two digits, in places 4 and 5, from MD5 are be used for the final calculation. However, instead of limiting this level to 64 it should be increased to 128 in order to increase the total amount of buckets and decrease the total amount of data per bucket. Also, note that from a given top level directory, only a total of: $65 \times 128 = 8192$ subdirectories are created, which is well below most file system limitations¹⁶. Graph M3 shows the distribution at the third and final level.

¹⁵File system limits depend on the filesystem; it is assumed that the readers are using fairly modern file systems.

¹⁶Again, this depends on the particular file system. Some major NAS devices have limits of 64,000 files per directory; make sure to be well below this limit.

Graph: M3



Mean: 2.27
Deviation: 1.51

Figure 8: Graph of the third level of the MD5 distribution.

As the graph M3 shows, the deviation is almost half of the mean. Normally this would not be ideal. However, at this level, the current data set is too small to fully fill all: $64 \times 64 \times 128 = 524,288$ buckets. Regardless, even if the mean remained constant and the object inventory grew one thousands times, each bucket would only contain 2,300 objects¹⁷. This is much lower than the letter based scheme in which some buckets contain more than 25,000 objects.

It would seem that the distribution using MD5 is far superior to the other approaches we have examined. Also, the MD5 algorithm will provide us with enough buckets to avoid having to descend down further than three levels. The MD5 algorithm used to calculate a member's top level location would be:

1. MD5 the member's user name
2. Convert the first two characters, places 0 and 1, from the MD5 into an integer: x
3. Calculate: $a = x \bmod 64$. then use a and the member's users name to locate the users data

The MD5 algorithm used to calculate a member's third level location would be:

1. MD5 the member's user name
2. Convert the first two characters, places 0 and 1, from the MD5 into an integer: x
3. Convert characters in places 2 and 3 from the MD5 into an integer: y
4. Convert characters in places 4 and 5 from the MD5 into an integer: z

¹⁷Note: $2.27 \times 1000 \approx 2,300$

5. Calculate: $a = x \bmod 64$, $b = y \bmod 64$, $c = z \bmod 64$
6. The full data path would then be: `<NAS mount>/a/b/c/<user_name>`

4 Conclusion

In this paper we have examined several methods used to distribute a large growing member base across a finite amount of resources. From our data we have observed that the best algorithm to yield a fairly even distribution is to use the results of the MD5 hash of the member's user name. From the top level down to the third level the distribution will remain fairly even. Also, the MD5 distribution satisfies all initial constraints.

1. The algorithm does not require any external data sources other than the user name.
2. Processing MD5 strings is not very expensive for small strings such as user names¹⁸.
3. The algorithm in general is platform agnostic.
4. Most popular scripting languages have built in support for MD5¹⁹. Therefore, its very easy to implement within a scripting language.
5. For Fotologs implementation, the MD5 algorithm will provide enough buckets to avoid having to descend down further than three levels.
6. We have seen from the graphs that this will scale well beyond 1 billion members.
7. It is a one to one function²⁰.

I have to admit that using MD5, or hashing functions in general, to distribute data is not unique. And I am not trying to take credit for it. After doing my research and writing this paper, I have seen what appear to be similar approaches. However, I have not found any source that documents this approach. Therefore, I still felt that this paper was worth writing and publishing even if its only for documentation purposes.

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\$RCSfile: md5_algo.lyx,v \$,\$Revision: 1.12 \$

¹⁸R. Rivest, rfc1321, 1992.

¹⁹As of writing: PHP, Perl, Tcl, and Python support MD5. Others can be found at: <http://userpages.umbc.edu/~mabzug1/cs/md5/md5.html>

²⁰MD5 was designed to be a message-digest algorithm and is known to have collision weaknesses. These can be avoided by using the full user name as the final data location (ex: `/a/b/c/<user_name>`) and therefore claim this mapping to be one to one.